

A Search for $B \rightarrow K^{(*)}\nu\bar{\nu}$ and Invisible Quarkonium Decays

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We search for the flavor-changing neutral-current decays $B \rightarrow K^{(*)}\nu\bar{\nu}$, and the invisible decays $J/\psi \rightarrow \nu\bar{\nu}$ and $\psi(2S) \rightarrow \nu\bar{\nu}$ via $B \rightarrow K^{(*)}J/\psi$ and $B \rightarrow K^{(*)}\psi(2S)$ respectively, using a data sample of 471×10^6 $B\bar{B}$ pairs collected by the BABAR experiment. We fully reconstruct the hadronic decay of one of the B mesons in the $\Upsilon(4S) \rightarrow B\bar{B}$ decay, and search for the $B \rightarrow K^{(*)}\nu\bar{\nu}$ decay in the rest of the event. We observe no significant excess of signal decays over background and report branching fraction upper limits of $\mathcal{B}(B^+ \rightarrow K^+\nu\bar{\nu}) < 3.7 \times 10^{-5}$, $\mathcal{B}(B^0 \rightarrow K^0\nu\bar{\nu}) < 8.1 \times 10^{-5}$, $\mathcal{B}(B^+ \rightarrow K^{*+}\nu\bar{\nu}) < 11.6 \times 10^{-5}$, $\mathcal{B}(B^0 \rightarrow K^{*0}\nu\bar{\nu}) < 9.3 \times 10^{-5}$, and combined upper limits of $\mathcal{B}(B \rightarrow K\nu\bar{\nu}) < 3.2 \times 10^{-5}$ and $\mathcal{B}(B \rightarrow K^*\nu\bar{\nu}) < 7.9 \times 10^{-5}$, all at the 90% confidence level. For the invisible quarkonium decays, we report branching fraction upper limits of $\mathcal{B}(J/\psi \rightarrow \nu\bar{\nu}) < 3.9 \times 10^{-3}$ and $\mathcal{B}(\psi(2S) \rightarrow \nu\bar{\nu}) < 15.5 \times 10^{-3}$ at the 90% confidence level. Using the improved kinematic resolution achieved from hadronic reconstruction, we also provide partial branching fraction limits for the $B \rightarrow K^{(*)}\nu\bar{\nu}$ decays over the full kinematic spectrum.

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INTRODUCTION

Flavor-changing neutral-current (FCNC) transitions, such as $b \rightarrow s\nu\bar{\nu}$, are prohibited in the Standard Model (SM) at tree-level. However, they can occur via one-loop box or electroweak penguin diagrams, as shown in Fig. 1. They can occur also in the SM via a quarkonium resonance state $b \rightarrow s\bar{c}c$, $\bar{c}c \rightarrow \nu\bar{\nu}$, where the $\bar{c}c$ decay is mediated by a virtual Z^0 boson (Fig. 2). This latter decay process has the same final state as $b \rightarrow s\nu\bar{\nu}$ with an additional constraint from the on-shell $\bar{c}c$ mass. Both the $b \rightarrow s\nu\bar{\nu}$ and $\bar{c}c \rightarrow \nu\bar{\nu}$ decay rates are expected to be small within the SM, with branching fractions estimated to be $\mathcal{B}(B^+ \rightarrow K^+\nu\bar{\nu}) = \mathcal{B}(B^0 \rightarrow K^0\nu\bar{\nu}) = (4.5 \pm 0.7) \times 10^{-6}$, $\mathcal{B}(B^+ \rightarrow K^{*+}\nu\bar{\nu}) = \mathcal{B}(B^0 \rightarrow K^{*0}\nu\bar{\nu}) = (6.8_{-1.1}^{+1.0}) \times 10^{-6}$ [1], and $\mathcal{B}(J/\psi \rightarrow \nu\bar{\nu}) = (4.54 \times 10^{-7}) \cdot \mathcal{B}(J/\psi \rightarrow e^+e^-)$ [2]. The $b \rightarrow s\nu\bar{\nu}$ rates are predicted with smaller theoretical uncertainties than those in the corresponding $b \rightarrow s\ell^+\ell^-$ modes due to the absence of long-distance hadronic effects from electromagnetic penguin contributions.

Various new-physics scenarios exist that could significantly enhance the $b \rightarrow s\nu\bar{\nu}$ branching fractions, as well as modify the expected SM decay distributions of $s_B \equiv q^2/m_B^2$, where q^2 is the squared magnitude of the four-momentum transferred from the B meson to

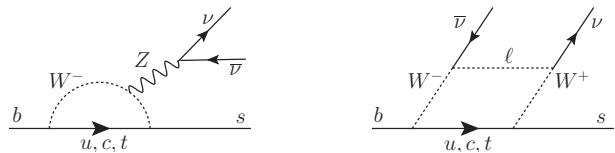


FIG. 1: Lowest-order SM Feynman diagrams for $b \rightarrow s\nu\bar{\nu}$ transitions. The virtual top quark provides the dominant contribution in each case.

the neutrino pair, and m_B is the B meson mass. Some of these scenarios predict massive particles that could contribute additional loop diagrams with similar amplitudes as those in the SM, such as nonstandard Z^0 couplings with supersymmetric (SUSY) particles [1], fourth-generation quarks [3], anomalous top-charm transitions [4], or a massive U(1) gauge boson Z' [1, 5]. Since $b \rightarrow s\nu\bar{\nu}$ has two final-state neutrinos, other sources of new physics can also contribute to the experimental signature of a kaon and missing four-momentum, such as low-mass dark-matter (LDM) candidates [1, 6–8], unparticles [9], right-handed neutrinos [5], or SUSY particles [10]. Models with a single universal extra dimension also predict higher decay rates [11].

The decays $J/\psi \rightarrow \nu\bar{\nu}$ and $\psi(2S) \rightarrow \nu\bar{\nu}$ provide additional windows for new-physics searches. In

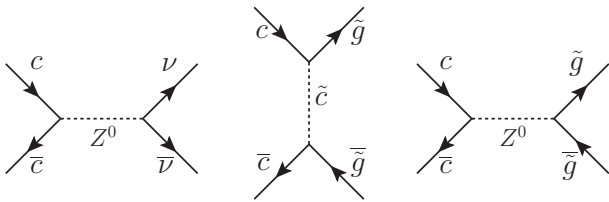


FIG. 2: Lowest-order Feynman diagrams of (from left to right) the SM decay $c\bar{c} \rightarrow \nu\bar{\nu}$, the SUSY decay $c\bar{c}$ into a pair of goldstinos (\tilde{g}) via a c -squark in the t-channel, and the SUSY decay $c\bar{c} \rightarrow \tilde{g}\bar{\tilde{g}}$ via a virtual Z^0 in the s-channel.

spontaneously-broken SUSY, a $c\bar{c}$ resonance can decay into a pair of goldstinos via either a virtual Z^0 in the s-channel or a c -squark exchange in the t-channel [2] (Fig. 2). The contribution of a massive SU(2) gauge boson Z' , introduced in the left-right SUSY model, could suppress the decay rates up to an order of magnitude [2]. Conversely, a low-mass U(1) gauge boson U could enhance the invisible decay rates of quarkonium states by several orders of magnitude by coupling to LDM particles [12, 13]. The U boson could decay into a pair of spin-1/2 Majorana ($\chi\chi$), spin-1/2 Dirac ($\chi\bar{\chi}$), or spin-0 ($\varphi\varphi$) LDM particles.

We search for $B \rightarrow K\nu\bar{\nu}$ and $B \rightarrow K^*\nu\bar{\nu}$, and for $J/\psi \rightarrow \nu\bar{\nu}$ and $\psi(2S) \rightarrow \nu\bar{\nu}$ via $B \rightarrow K^{(*)}J/\psi$ and $B \rightarrow K^{(*)}\psi(2S)$ respectively, where $K^{(*)}$ signifies a charged or neutral K or K^* meson [14]. We use a technique in which one B meson is exclusively reconstructed in a hadronic final state before looking for a signal decay within the rest of the event. Since the four-momentum of one B meson is fully determined, the missing mass resolution on the two final-state neutrinos and the suppression of background are improved with respect to other reconstruction techniques.

Several previous searches for $B \rightarrow K\nu\bar{\nu}$ and $B \rightarrow K^*\nu\bar{\nu}$ have been performed by both the BABAR and BELLE collaborations [15–18]. Currently, the most stringent published upper limits at 90% confidence level (CL) are $\mathcal{B}(B^+ \rightarrow K^+\nu\bar{\nu}) < 1.3 \times 10^{-5}$ [17] and $\mathcal{B}(B \rightarrow K^*\nu\bar{\nu}) < 8 \times 10^{-5}$ [18]. The $\mathcal{B}(B^+ \rightarrow K^+\nu\bar{\nu})$ limit was determined using semileptonic-tag reconstruction, which produces samples that are statistically larger and independent of those produced using the hadronic-tag reconstruction employed in this search. The $\mathcal{B}(B \rightarrow K^*\nu\bar{\nu})$ limit was a combination of two BABAR analyses, one using semileptonic-tag reconstruction and the other using hadronic-tag reconstruction.

A $J/\psi \rightarrow \nu\bar{\nu}$ search via $\psi(2S) \rightarrow \pi\pi J/\psi$ was performed by the BES collaboration, which set an upper limit at 90% CL of $\mathcal{B}(J/\psi \rightarrow \nu\bar{\nu}) < 1.2 \times 10^{-2} \cdot \mathcal{B}(J/\psi \rightarrow \mu^+\mu^-)$ [19]. This article presents the first search for $J/\psi \rightarrow \nu\bar{\nu}$ using the hadronic-tag reconstruction of a B meson decay. A search for $\psi(2S) \rightarrow \nu\bar{\nu}$ has not been performed previously.

THE BABAR DETECTOR AND DATA SAMPLE

This search uses a data sample of 471 ± 3 million $B\bar{B}$ pairs, corresponding to an integrated luminosity of 429 fb^{-1} collected at the $\Upsilon(4S)$ resonance [20]. The data were recorded with the BABAR detector [21] at the PEP-II asymmetric-energy e^+e^- storage rings. The charged-particle tracking system consists of a five-layer double-sided silicon vertex tracker and a 40-layer drift chamber, both coaxial with a 1.5 T solenoidal magnetic field. Charged kaons and pions are distinguished by specific ionization energy-loss measurements from the tracking system for lower momentum particles, and by measurements from a ring-imaging Cherenkov radiation detector for higher momentum particles. A CsI(Tl) electromagnetic calorimeter is used to reconstruct photons of energy greater than 20 MeV and to identify electrons. Muon identification is provided by the instrumented flux return of the magnet. Particle identification (PID) algorithms are trained to identify charged particle types by using 36 input parameters including momentum, polar and azimuthal angles, the Cherenkov angle, and energy-loss measurements [22]. We employ PID criteria that select K^+ mesons with an efficiency greater than 85% and with approximately 1% misidentification probability for pions and muons.

Signal and background decays are studied using Monte Carlo (MC) samples simulated with Geant4 [23]. The simulation includes a detailed model of the BABAR detector geometry and response. Beam-related background and detector noise are extracted from data and are overlaid on the MC simulated events. Large MC samples of generic $B\bar{B}$ and continuum ($e^+e^- \rightarrow \tau^+\tau^-$ or $e^+e^- \rightarrow q\bar{q}$, where $q = u, d, s, c$) events provide ten times the number of $\Upsilon(4S) \rightarrow B\bar{B}$ and $e^+e^- \rightarrow c\bar{c}$ events as in the data sample, and four times the number of other continuum decays. The $\Upsilon(4S) \rightarrow B\bar{B}$ signal MC samples are generated with one B meson decaying via $B \rightarrow K^{(*)}\nu\bar{\nu}$, with and without the $c\bar{c}$ resonances, while the other B meson decays according to a model tuned to world averages of allowed decay channels. The s_B distributions for $B \rightarrow K^{(*)}\nu\bar{\nu}$ decays within signal MC samples are generated initially using a phase-space model, and then reweighted using the model from Ref. [1], henceforth referred to as ABSW. Within $B \rightarrow K^*\nu\bar{\nu}$ decays, this model is also used to reweight the helicity-angle distribution between the signal B and the K^+ or K^0 flight directions in the K^* rest frame. The helicity amplitudes for the decay channels $B \rightarrow K^*J/\psi$ and $B \rightarrow K^*\psi(2S)$ are generated using values taken from a BABAR measurement [24].

ANALYSIS METHOD

Event selection for both the $B \rightarrow K^{(*)}\nu\bar{\nu}$ and $B \rightarrow K^{(*)}c\bar{c}$, $c\bar{c} \rightarrow \nu\bar{\nu}$ searches begins by fully reconstructing a B meson (B_{tag}) in one of many hadronic final states, $\bar{B} \rightarrow SX_{\text{had}}^-$, where S is a “seed” meson ($D^{(*)+}$, $D^{(*)0}$, $D_s^{(*)+}$, or J/ψ) and X_{had}^- is a collection of at most five mesons, composed of charged and neutral kaons and pions with a net charge of -1 . This method, which was used also in Ref. [25], reconstructs additional modes with respect to previous hadronic-tag $B \rightarrow K^{(*)}\nu\bar{\nu}$ analyses [15, 18], and results in approximately twice the reconstruction efficiency. The D seeds are reconstructed in the decay modes $D^+ \rightarrow K_S^0\pi^+$, $K_S^0\pi^+\pi^0$, $K_S^0\pi^+\pi^+\pi^-$, $K^-\pi^+\pi^+$, $K^-\pi^+\pi^+\pi^0$, $K^+K^-\pi^+$, $K^+K^-\pi^+\pi^0$; $D^0 \rightarrow K^-\pi^+$, $K^-\pi^+\pi^0$, $K^-\pi^+\pi^+\pi^-$, $K_S^0\pi^+\pi^-$, $K_S^0\pi^+\pi^-\pi^0$, K^+K^- , $\pi^+\pi^-$, $\pi^+\pi^-\pi^0$, and $K_S^0\pi^0$. Additional seeds are reconstructed as $D^{*+} \rightarrow D^0\pi^+$, $D^+\pi^0$; $D^{*0} \rightarrow D^0\pi^0$, $D^0\gamma$; $D_s^{*+} \rightarrow D_s^+\gamma$; $D_s^+ \rightarrow \phi[\rightarrow K^+K^-]\pi^+$, $K_S^0K^+$; and $J/\psi \rightarrow e^+e^-$, $\mu^+\mu^-$. The K_S^0 candidates are reconstructed via their decay to $\pi^+\pi^-$.

Well-reconstructed B_{tag} candidates are selected using two kinematic variables: $\Delta E = E_{B_{\text{tag}}} - \sqrt{s}/2$ and $m_{\text{ES}} = \sqrt{s/4 - \vec{p}_{B_{\text{tag}}}^2}$, where $E_{B_{\text{tag}}}$ and $\vec{p}_{B_{\text{tag}}}$ are the energy and momentum vector of the B_{tag} candidate, respectively, in the e^+e^- center-of-mass (CM) frame and \sqrt{s} is the total energy of the e^+e^- system. The value of ΔE , which peaks at zero for correctly reconstructed B mesons, is required to be between -0.12 and 0.12 GeV or within two standard deviations around the mean for a given X_{had}^- mode, whichever is the tighter constraint. If more than one B_{tag} candidate is reconstructed, the one in the mode with the highest purity (fraction of candidates that are correctly reconstructed within a given B_{tag} decay mode) is chosen. If there are multiple candidates with the same purity, the one with the smallest $|\Delta E|$ is selected.

After requiring that the event contains between one and three tracks not used in the B_{tag} reconstruction (“signal-side” tracks), the purity of each mode is recalculated, and only the B_{tag} modes that have a recalculated purity greater than 68% are retained. This results in a total of 448 final states. This purity value was optimized by maximizing the figure of merit [26]

$$\frac{\varepsilon_i^{\text{sig}}}{\frac{1}{2}n_\sigma + \sqrt{N_i^{\text{bkg}}}}, \quad (1)$$

where the number of sigmas $n_\sigma = 1.28$ corresponds to a one-sided Gaussian limit at 90% CL, $\varepsilon_i^{\text{sig}}$ is the total signal efficiency, and N_i^{bkg} is the expected number of background events, with i representing one of the signal decay channels. All other selection criteria discussed henceforth were optimized simultaneously using this same figure of merit.

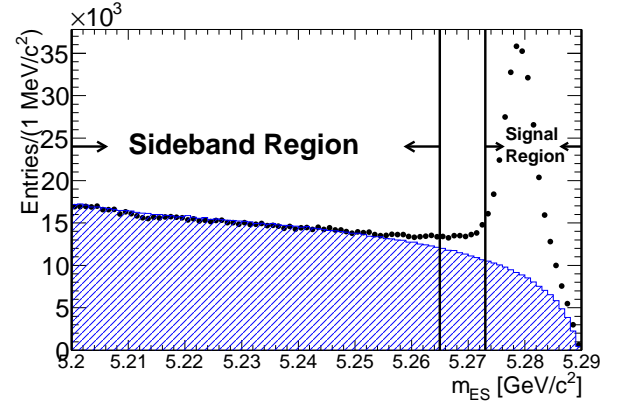


FIG. 3: The m_{ES} distribution for the B_{tag} candidates in data (points) and in the expected combinatorial background as predicted by the MC (shaded). This distribution includes only the charged and neutral B_{tag} candidates that pass the purity restrictions, the multivariate continuum suppression, and a requirement of one to three signal-side tracks. The data within the m_{ES} sideband region is used to extrapolate the expected number of combinatorial background events within the signal region.

The signal region of the B_{tag} candidate is defined as $5.273 < m_{\text{ES}} < 5.290$ GeV/ c^2 (Fig. 3), since correctly reconstructed B mesons produce a peak in this region near the nominal B -meson mass. The B_{tag} candidates that are incorrectly reconstructed (“combinatorial” events), which result from continuum events or are due to tracks or clusters assigned to the wrong B meson, produce a distribution that is relatively uniform below the m_{ES} signal region and decreases toward the kinematic limit within it. Approximately 0.3% of signal MC events and 12.0 million data events contain a B_{tag} that is reconstructed using the above requirements and found to be within the m_{ES} signal region.

Since B mesons are spin zero and are produced with low momentum in the CM frame (~ 0.32 GeV/ c), their decay products are more isotropically distributed than non- $B\bar{B}$ background. For example, $|\cos\theta_T|$, where θ_T is the angle in the CM frame between the B_{tag} thrust [27] axis and the thrust axis of all other particles in the event, has a uniform distribution for $B\bar{B}$ events but peaks near one for continuum events. Continuum background is suppressed by using a multivariate likelihood selector based on six event-shape variables. These consist of $|\cos\theta_T|$, the cosine of the angle between $\vec{p}_{B_{\text{tag}}}$ and the beam axis, the magnitude of the B_{tag} thrust, the component of the B_{tag} thrust along the beam axis, the angle between the missing momentum vector (\vec{p}_{miss}) and the beam axis, and the ratio of the second-to-zeroth Fox-Wolfram moment [28] computed using all charged and neutral particles in the

event. The multivariate selector requires

$$\mathcal{L}_B \equiv \frac{\prod_j \mathcal{P}_B(x_j)}{\prod_j \mathcal{P}_B(x_j) + \prod_j \mathcal{P}_q(x_j)} > 53\%, \quad (2)$$

where $\mathcal{P}_q(x_j)$ and $\mathcal{P}_B(x_j)$ are probability density functions determined from MC that describe continuum and signal-like $B\bar{B}$ events, respectively, for the six event-shape variables x_j . The \mathcal{L}_B requirement, which was optimized with other selection criteria using Eq. (1), also improves the agreement between data and MC by suppressing unmodeled continuum backgrounds.

In the sample of selected B_{tag} candidates, signal events are chosen such that all of the remaining tracks can be combined to yield a single $K^{(*)}$ candidate. The sum of the $K^{(*)}$ and B_{tag} candidate charges must equal zero. Since signal decays have two final-state neutrinos, these events are required to have missing energy greater than zero, where the missing energy is defined as the CM energy minus all detected calorimeter deposits from charged and neutral particles in the event. For $B \rightarrow K^{(*)}\nu\bar{\nu}$, the signal decays are reconstructed in six channels: $B^+ \rightarrow K^+\nu\bar{\nu}$; $B^0 \rightarrow K^0\nu\bar{\nu}$ where $K^0 \rightarrow K_S^0$; $B^+ \rightarrow K^{*+}\nu\bar{\nu}$, where $K^{*+} \rightarrow K^+\pi^0$ and $K^{*+} \rightarrow K_S^0\pi^+$; and $B^0 \rightarrow K^{*0}\nu\bar{\nu}$, where $K^{*0} \rightarrow K^+\pi^-$ and $K^{*0} \rightarrow K_S^0\pi^0$. For $c\bar{c} \rightarrow \nu\bar{\nu}$, the same six signal channels are employed with an additional requirement that the $K^{(*)}$ momentum is consistent with a two-body decay, either $B \rightarrow K^{(*)}J/\psi$ or $B \rightarrow K^{(*)}\psi(2S)$. The J/ψ and $\psi(2S)$ mesons then decay into a pair of neutrinos, thus yielding the same final states as for $B \rightarrow K^{(*)}\nu\bar{\nu}$.

We reconstruct $K_S^0 \rightarrow \pi^+\pi^-$ decay candidates using two tracks of opposite charge, which originate from a common vertex and produce an invariant mass within $\pm 7 \text{ MeV}/c^2$ of the nominal K_S^0 mass [29]. The PID for each track must be inconsistent with that for an electron, muon, or kaon. The π^0 candidates are reconstructed from pairs of photon candidates with individual energies greater than 30 MeV, a total CM energy greater than 200 MeV, and a $\gamma\gamma$ invariant mass between 100 and 160 MeV/c^2 . All K^+ candidates must satisfy the PID criteria for a kaon.

Reconstructed K^* candidates are required to have an invariant mass within $\pm 70 \text{ MeV}/c^2$ of the nominal K^* mass [29]. A $K^{*+} \rightarrow K_S^0\pi^+$ candidate combines a K_S^0 candidate with a track that satisfies the PID criteria for a pion. If more than one $K^{*+} \rightarrow K_S^0\pi^+$ candidate can be reconstructed in an event, the one with the mass closest to the nominal K^{*+} mass is chosen. A $K^{*0} \rightarrow K^+\pi^-$ candidate combines one track that satisfies the PID criteria for a kaon with one that is inconsistent with the PID criteria for an electron, muon, or kaon. In an event containing a K^+ (K_S^0) candidate and no additional signal-side tracks, $K^* \rightarrow K^+\pi^0$ ($K_S^0\pi^0$) candidates are reconstructed if the invariant mass of a π^0 candidate and the K^+ (K_S^0) candidate falls within the K^* mass window;

otherwise the event is considered for the K^+ (K_S^0) signal channel. If more than one $K^{*+} \rightarrow K^+\pi^0$ or $K^{*0} \rightarrow K_S^0\pi^0$ candidate can be reconstructed, the one with the highest energy π^0 candidate is chosen.

Once the B_{tag} and $K^{(*)}$ are identified, the signal events are expected to contain little or no additional energy within the calorimeter. However, additional energy deposits can result from beam-related photons, hadronic shower fragments that were not reconstructed into the primary particle deposit, and photons from unreconstructed $D^* \rightarrow D\gamma/\pi^0$ transitions in the B_{tag} candidate. Only deposits with energy greater than 50 MeV in the rest frame of the detector are considered, and the sum of all such additional energy deposits (E_{extra}) is required to be less than a threshold value (E_i). The values of E_i , given in Table I, were optimized with the other selection criteria but were allowed to differ between signal channels. For events within the K^+ signal channel, clusters identified as kaon shower fragments are not included in the E_{extra} sum. A fragment candidate is defined as a cluster whose momentum vector, when compared to that of the signal track, is separated by polar and azimuthal angles (relative to the beam axis and in the rest frame of the detector) of $\Delta\theta$ and $\Delta\phi$, respectively, such that $r_{\text{clus}} < 15^\circ$, where $r_{\text{clus}} \equiv \sqrt{(\Delta\theta)^2 + \frac{2}{3}(Q_K \cdot \Delta\phi - 8^\circ)^2}$ and $Q_K = \pm 1$ is the K^\pm charge. The r_{clus} and fragment candidate definitions were optimized using studies of truth information in the signal MC samples. The recovery of these kaon shower fragments improves the final signal efficiency in the K^+ channel by about 13%. This procedure was explored for the other signal tracks, but the effect was small.

TABLE I: Threshold values E_i for the E_{extra} variable in each of the signal channels, determined using Eq. (1). The channels in brackets refer to the K^* decay products.

Channel	K^+	K^0	$[K^+\pi^0]$	$[K_S^0\pi^+]$	$[K^+\pi^-]$	$[K_S^0\pi^0]$
E_i [GeV]	0.11	0.28	0.18	0.29	0.31	0.33

The searches for $B \rightarrow K^{(*)}\nu\bar{\nu}$ and for $c\bar{c} \rightarrow \nu\bar{\nu}$ via $B \rightarrow K^{(*)}c\bar{c}$ diverge in the final step of the signal selection, which involves restricting the kinematics of the decay. The value of s_B is calculated as $(p_{B_{\text{sig}}} - p_{K^{(*)}})^2/m_B^2$, where $p_{K^{(*)}}$ is the four-momentum of the $K^{(*)}$ candidate, and $p_{B_{\text{sig}}}$ is the expected signal B four-momentum with an energy of $\sqrt{s}/2$, the nominal B -meson mass, and a momentum vector pointing opposite the B_{tag} momentum. For $B \rightarrow K^{(*)}\nu\bar{\nu}$, the signal region optimized for maximum SM sensitivity is $0 < s_B < 0.3$ for all six signal channels. This corresponds to a $K^{(*)}$ momentum greater than about 1.8 (1.7) GeV/c in the signal B rest frame for $B \rightarrow K\nu\bar{\nu}$ ($B \rightarrow K^*\nu\bar{\nu}$) events. Partial branching fractions over the full s_B range are also provided

for sensitivity to new-physics scenarios that modify the kinematic distributions for $B \rightarrow K^{(*)}\nu\bar{\nu}$. For $c\bar{c} \rightarrow \nu\bar{\nu}$ via $B \rightarrow K^{(*)}c\bar{c}$, the invariant mass of the two neutrinos $m_{\nu\bar{\nu}} \equiv \sqrt{s_B m_B^2}$ is expected to correspond to the mass of the J/ψ (3.097 GeV/ c^2) meson or to that of the $\psi(2S)$ (3.686 GeV/ c^2) meson. Signal events are selected within three standard deviations around the nominal $c\bar{c}$ masses, which results in windows of $3.044 < m_{\nu\bar{\nu}} < 3.146$ ($3.019 < m_{\nu\bar{\nu}} < 3.175$) GeV/ c^2 for the $B \rightarrow KJ/\psi$ ($B \rightarrow K^*J/\psi$) channel, and $3.650 < m_{\nu\bar{\nu}} < 3.724$ ($3.627 < m_{\nu\bar{\nu}} < 3.739$) GeV/ c^2 for the $B \rightarrow K\psi(2S)$ ($B \rightarrow K^*\psi(2S)$) channel.

To avoid experimenter bias, all the above selection criteria and values were optimized using the MC before looking at any data events within the E_{extra} and m_{ES} signal regions.

BACKGROUND AND BRANCHING FRACTION EXTRACTION

The total number of background events N_i^{bkg} in the signal region has two components: N_i^{peak} is the number of expected background events having a correctly reconstructed B_{tag} candidate and hence peaking within the m_{ES} signal region, and N_i^{comb} is the number of expected combinatorial background events, including both continuum events and $B\bar{B}$ events with an incorrectly reconstructed B_{tag} candidate. To reduce the dependence on MC simulations, the number of N_i^{comb} events is extrapolated directly from the observed data events within the m_{ES} sideband region, defined as $5.200 < m_{\text{ES}} < 5.265$ GeV/ c^2 and depicted in Fig. 3. The shape of the combinatorial m_{ES} distribution is estimated using MC samples of continuum events and of $B\bar{B}$ events reconstructed with the wrong charge.

The number of N_i^{peak} events is estimated from generic $B\bar{B}$ MC samples. Over half of N_i^{peak} is found to be from $B \rightarrow D^{(*)}\ell\nu$ ($\ell = e$ or μ) decays in which no lepton candidate is identified in the event and the $K^{(*)}$ is a daughter of the D or D^* meson. One particular peaking background in the $B \rightarrow K^{(*)}\nu\bar{\nu}$ search is $B^+ \rightarrow \tau^+\nu_\tau$, with $\tau^+ \rightarrow K^{(*)+}\nu_\tau$, which has the same final state as the signal decay [30]. Exclusive $B^+ \rightarrow \tau^+\nu_\tau$ MC samples, assuming a branching fraction of $(1.65 \pm 0.34) \times 10^{-4}$ [29], indicate that this background constitutes less than 15 (5)% of the total background in the $B^+ \rightarrow K^+\nu\bar{\nu}$ ($B^+ \rightarrow K^{*+}\nu\bar{\nu}$) channel.

Since both N_i^{peak} and $\varepsilon_i^{\text{sig}}$ are determined from MC samples, we normalize the MC yields to the data to account for differences between data and MC, such as from the B_{tag} reconstruction and the modeled branching fractions of B_{tag} modes within the MC. This normalization is performed before applying the full signal selection in order to have a large background-to-signal ratio; looser $K^{(*)}$ mass windows and E_{extra} selection requirements are

used such that the number of background events is approximately 60 times larger than the final background contribution, over the full s_B spectrum. The peaking background component in the $B\bar{B}$ MC is then normalized to the number of data events that peak within the m_{ES} signal region. This peaking yield normalization is performed separately for charged and neutral B_{tag} candidates, and results in the scaling of all signal and background MC samples by 1.027 ± 0.039 (1.017 ± 0.044) for charged (neutral) B_{tag} candidates.

The signal branching fractions are calculated using

$$\mathcal{B}_i = \frac{N_i^{\text{obs}} - (N_i^{\text{peak}} + N_i^{\text{comb}})}{\varepsilon_i^{\text{sig}} N_{B\bar{B}}}, \quad (3)$$

where $N_{B\bar{B}} = 471 \times 10^6$ is the total number of B meson pairs in the data sample and N_i^{obs} is the number of data events within the signal region. The total signal efficiency $\varepsilon_i^{\text{sig}}$ includes that of the B_{tag} reconstruction and is determined separately for each of the signal channels i . Since misreconstructed events from other signal channels contribute to N_i^{peak} , the branching fractions of all signal channels are determined simultaneously. Branching fraction limits and uncertainties are computed using a mixed frequentist-Bayesian approach described in Ref. [31], with the systematic uncertainties on N_i^{bkg} and $\varepsilon_i^{\text{sig}}$ modeled using Gaussian distributions. To combine the results of signal decay channels, we find the \mathcal{B}_i value that maximizes a likelihood function defined as the product of the Poisson probabilities of observing N_i^{obs} events.

SYSTEMATIC STUDIES

To verify the modeling of $\varepsilon_i^{\text{sig}}$ and N_i^{bkg} , a control sample of $B \rightarrow D\ell\nu$ events is selected. In place of a signal K^* candidate, the events are required to contain a reconstructed $D^0 \rightarrow K^-\pi^+$, $D^- \rightarrow K^+\pi^-\pi^-$, or $D^- \rightarrow K_S^0\pi^-\pi^-$ candidate with an invariant mass within ± 35 MeV/ c^2 of the nominal D -meson mass values [29]. The event must have one additional track that satisfies the PID criteria of either an electron or muon. All other reconstruction and signal selection requirements are retained. The resulting yields in the data agree with MC expectations, assuming the well-measured branching fractions of $B \rightarrow D\ell\nu$ [29], within the 7% (12%) statistical uncertainty of the data in the $0 < s_B < 0.3$ (J/ψ or $\psi(2S)$ mass) region.

The control sample is used to determine the systematic uncertainties due to the MC modeling of the E_{extra} variable within data. Additional uncertainties on N_i^{peak} and $\varepsilon_i^{\text{sig}}$ are due to the K_S^0 and K^* mass reconstruction windows, the π^0 reconstruction, and the uncertainties in the branching fractions [29] of the dominant backgrounds contributing to N_i^{peak} . The uncertainty on N_i^{comb} is dominated by the sideband data statistics. Other systematic

uncertainties, such as those from PID, tracking, B_{tag} reconstruction, $N_{B\bar{B}}$, and the assumption that charged and neutral $B\bar{B}$ pairs are produced at equal rates, are all accounted for by the normalization of the MC peaking yields. Because the peaking yield in data depends on the extrapolated shape of the combinatorial B_{tag} background, the normalization scale factors are re-evaluated by varying the method used to extrapolate this shape. The resulting variations on the final N_i^{bkg} and $\varepsilon_i^{\text{sig}}$ values are taken as the systematic uncertainties due to the normalization.

Due to the approximately 1.0% resolution on the s_B measurement around $s_B = 0.3$, an uncertainty is evaluated within the $B \rightarrow K^{(*)}\nu\bar{\nu}$ signal region. Similarly, the resolution on $m_{\nu\bar{\nu}}$ contributes to uncertainties within the $J/\psi \rightarrow \nu\bar{\nu}$ and $\psi(2S) \rightarrow \nu\bar{\nu}$ signal regions. Only the systematic uncertainties due to the N_i^{peak} branching fractions and to s_B or $m_{\nu\bar{\nu}}$ differ between the $B \rightarrow K^{(*)}\nu\bar{\nu}$, $J/\psi \rightarrow \nu\bar{\nu}$, and $\psi(2S) \rightarrow \nu\bar{\nu}$ searches. The systematic uncertainties are summarized in Tables II and III; the former lists the uncertainties shared by the searches, while the latter lists those that differ.

RESULTS FOR $B \rightarrow K^{(*)}\nu\bar{\nu}$

Figure 4 shows the observed data yields, expected background contributions, and SM signal distributions over the full s_B spectrum. Tables IV and V summarize the number of observed data events within the s_B signal region ($0 < s_B < 0.3$), expected backgrounds, $B \rightarrow K^{(*)}\nu\bar{\nu}$ signal efficiencies, branching fraction central values, and branching fraction limits at the 90% CL. Combining the signal channels, we determine upper limits of $\mathcal{B}(B \rightarrow K\nu\bar{\nu}) < 3.2 \times 10^{-5}$ and $\mathcal{B}(B \rightarrow K^*\nu\bar{\nu}) < 7.9 \times 10^{-5}$. Since we see a small excess over the expected background in the K^+ channel, we report a two-sided 90% confidence interval. However, the probability of observing such an excess within the signal region, given the uncertainty on the background, is 8.4% which corresponds to a one-sided Gaussian significance of about 1.4σ . Therefore, this excess is not considered significant.

Using the same procedure as when combining signal decay channels, the $B \rightarrow K\nu\bar{\nu}$ branching fraction central values are combined with a previous semileptonic-tag *BABAR* analysis that searched within a statistically independent data sample [17]. We obtain combined *BABAR* upper limits at the 90% CL of

$$\begin{aligned} \mathcal{B}(B^+ \rightarrow K^+\nu\bar{\nu}) &< 1.6 \times 10^{-5}, \\ \mathcal{B}(B^0 \rightarrow K^0\nu\bar{\nu}) &< 4.9 \times 10^{-5}, \text{ and} \\ \mathcal{B}(B \rightarrow K\nu\bar{\nu}) &< 1.7 \times 10^{-5}. \end{aligned} \quad (4)$$

The combined central value is $\mathcal{B}(B \rightarrow K\nu\bar{\nu}) = (0.8_{-0.6}^{+0.7}) \times 10^{-5}$, where the uncertainty includes both statistical and systematic uncertainties. These combined

TABLE II: Summary of systematic uncertainties that are shared by the $B \rightarrow K^{(*)}\nu\bar{\nu}$, $J/\psi \rightarrow \nu\bar{\nu}$, and $\psi(2S) \rightarrow \nu\bar{\nu}$ searches. All values are relative uncertainties in %. The channels in brackets refer to the K^* decay products.

Source	K^+	$[K^+\pi^0]$	$[K_S^0\pi^+]$	K^0	$[K^+\pi^-]$	$[K_S^0\pi^0]$
$\varepsilon_i^{\text{sig}}$ normalization	3.5	3.5	3.5	8.9	8.9	8.9
N_i^{bkg} normalization	2.3	2.3	2.3	6.0	6.0	6.0
K_S^0 reconstruction	—	—	1.4	1.4	—	1.4
K^* reconstruction	—	2.8	2.8	—	2.8	2.8
π^0 reconstruction	—	3.0	—	—	—	3.0
E_{extra}	4.5	6.0	6.5	6.0	6.0	6.5

TABLE III: Summary of systematic uncertainties that differ between the $B \rightarrow K^{(*)}\nu\bar{\nu}$, $J/\psi \rightarrow \nu\bar{\nu}$, and $\psi(2S) \rightarrow \nu\bar{\nu}$ searches, and the total systematic uncertainties for each signal channel. All values are relative uncertainties in %. The total systematic uncertainties are determined by adding in quadrature each relevant uncertainty, including those listed in Table II.

Source	K^+	$[K^+\pi^0]$	$[K_S^0\pi^+]$	K^0	$[K^+\pi^-]$	$[K_S^0\pi^0]$
$B \rightarrow K^{(*)}\nu\bar{\nu}$						
N_i^{peak} \mathcal{B} 's	2.8	2.8	2.8	2.8	2.8	2.8
s_B resolution	3.6	3.6	3.6	3.6	3.6	3.6
Total N_i^{peak} syst.	6.8	8.9	8.8	9.7	10.0	10.9
Total N_i^{comb} syst.	2.3	2.3	2.3	6.0	6.0	6.0
Total $\varepsilon_i^{\text{sig}}$ syst.	6.7	8.8	8.8	11.4	11.7	12.4
$J/\psi \rightarrow \nu\bar{\nu}$						
N_i^{peak} \mathcal{B} 's	3.5	3.5	3.5	3.5	3.5	3.5
$m_{\nu\bar{\nu}}$ resolution	1.1	2.1	0.4	0.7	0.3	1.3
Total N_i^{peak} syst.	6.2	8.6	8.4	9.3	9.6	10.5
Total N_i^{comb} syst.	2.3	2.3	2.3	6.0	6.0	6.0
Total $\varepsilon_i^{\text{sig}}$ syst.	5.8	8.3	8.0	10.8	11.1	11.9
$\psi(2S) \rightarrow \nu\bar{\nu}$						
N_i^{peak} \mathcal{B} 's	2.8	2.8	2.8	2.8	2.8	2.8
$m_{\nu\bar{\nu}}$ resolution	0.8	2.4	1.0	0.9	1.8	3.1
Total N_i^{peak} syst.	5.8	8.5	8.1	9.1	9.5	10.7
Total N_i^{comb} syst.	2.3	2.3	2.3	6.0	6.0	6.0
Total $\varepsilon_i^{\text{sig}}$ syst.	5.8	8.4	8.1	10.9	11.2	12.2

results reweight the s_B distribution to that of the ABSW theoretical model (dashed curve in Fig. 4), which decreases the signal efficiencies published in Ref. [17] by approximately 10%. The $B \rightarrow K^*\nu\bar{\nu}$ central values also can be combined with the semileptonic-tag results from a previous *BABAR* search [18]. In order to obtain approximate frequentist intervals, the likelihood functions in the previous search are extended to include possibly negative signals. We obtain combined *BABAR* upper limits at the

TABLE IV: Expected $B \rightarrow K^* \nu \bar{\nu}$ background yields $N_i^{\text{bkg}} = N_i^{\text{peak}} + N_i^{\text{comb}}$, signal efficiencies $\varepsilon_i^{\text{sig}}$, number of observed data events N_i^{obs} , resulting branching fraction upper limits at 90% CL, and the combined upper limits and central values, all within the $0 < s_B < 0.3$ region. Uncertainties are statistical and systematic, respectively. The channels in brackets refer to the K^* decay products.

	$B^+ \rightarrow [K^+ \pi^0] \nu \bar{\nu}$	$B^+ \rightarrow [K_S^0 \pi^+] \nu \bar{\nu}$	$B^0 \rightarrow [K^+ \pi^-] \nu \bar{\nu}$	$B^0 \rightarrow [K_S^0 \pi^0] \nu \bar{\nu}$
N_i^{peak}	$1.2 \pm 0.4 \pm 0.1$	$1.3 \pm 0.4 \pm 0.1$	$5.0 \pm 0.8 \pm 0.5$	$0.2 \pm 0.2 \pm 0.0$
N_i^{comb}	$1.1 \pm 0.4 \pm 0.0$	$0.8 \pm 0.3 \pm 0.0$	$2.0 \pm 0.5 \pm 0.1$	$0.5 \pm 0.3 \pm 0.0$
N_i^{bkg}	$2.3 \pm 0.5 \pm 0.1$	$2.0 \pm 0.5 \pm 0.1$	$7.0 \pm 0.9 \pm 0.5$	$0.7 \pm 0.3 \pm 0.0$
$\varepsilon_i^{\text{sig}} (\times 10^{-5})$	$4.9 \pm 0.2 \pm 0.4$	$6.0 \pm 0.2 \pm 0.5$	$12.2 \pm 0.3 \pm 1.4$	$1.2 \pm 0.1 \pm 0.1$
N_i^{obs}	3	3	7	2
Limit	$< 19.4 \times 10^{-5}$	$< 17.0 \times 10^{-5}$	$< 8.9 \times 10^{-5}$	$< 86 \times 10^{-5}$
$\mathcal{B}(B^{+ / 0} \rightarrow K^{*+ / 0} \nu \bar{\nu})$	$(3.3^{+6.2+1.7}_{-3.6-1.3}) \times 10^{-5}$		$(2.0^{+5.2+2.0}_{-4.3-1.7}) \times 10^{-5}$	
Limit	$< 11.6 \times 10^{-5}$		$< 9.3 \times 10^{-5}$	
$\mathcal{B}(B \rightarrow K^* \nu \bar{\nu})$	$(2.7^{+3.8+1.2}_{-2.9-1.0}) \times 10^{-5}$			
Limit	$< 7.9 \times 10^{-5}$			

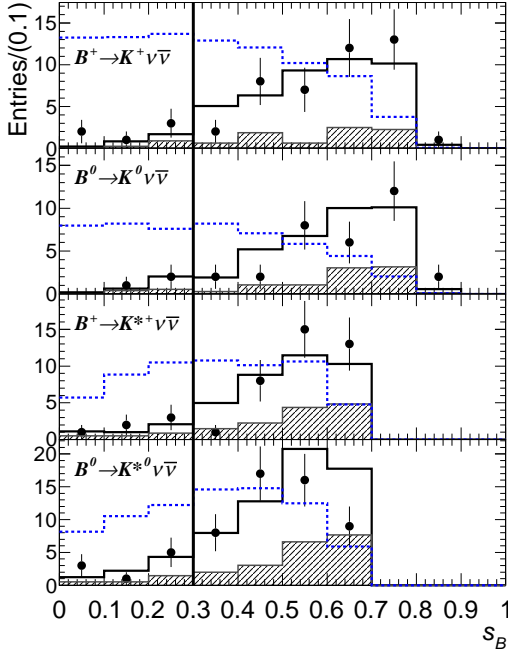


FIG. 4: The s_B distribution for (from top to bottom) $B^+ \rightarrow K^+ \nu \bar{\nu}$, $B^0 \rightarrow K^0 \nu \bar{\nu}$, $B^+ \rightarrow K^{*+} \nu \bar{\nu}$, and $B^0 \rightarrow K^{*0} \nu \bar{\nu}$ events after applying the full signal selection. The expected combinatorial (shaded) plus m_{ES} -peaking (solid) background contributions are overlaid on the data (points). The signal MC distribution (dashed) is normalized to a branching fraction of 20×10^{-5} for $B^+ \rightarrow K^+ \nu \bar{\nu}$ and 50×10^{-5} for the other channels. Events to the left of the vertical lines are selected to obtain SM-sensitive limits, while the full spectra are used to determine partial branching fractions.

TABLE V: Expected $B \rightarrow K \nu \bar{\nu}$ background yields $N_i^{\text{bkg}} = N_i^{\text{peak}} + N_i^{\text{comb}}$, signal efficiencies $\varepsilon_i^{\text{sig}}$, number of observed data events N_i^{obs} , resulting branching fraction upper limits at 90% CL, the central values \mathcal{B}_i , and the combined upper limits and central value, all within the $0 < s_B < 0.3$ region. Lower limits at 90% CL are also reported, as discussed in the text. Uncertainties are statistical and systematic, respectively. The $B^0 \rightarrow K^0 \nu \bar{\nu}$ efficiency accounts for $\mathcal{B}(K^0 \rightarrow K_S^0)$ and $\mathcal{B}(K_S^0 \rightarrow \pi^+ \pi^-)$ [29].

	$B^+ \rightarrow K^+ \nu \bar{\nu}$	$B^0 \rightarrow K^0 \nu \bar{\nu}$
N_i^{peak}	$1.8 \pm 0.4 \pm 0.1$	$2.0 \pm 0.5 \pm 0.2$
N_i^{comb}	$1.1 \pm 0.4 \pm 0.0$	$0.9 \pm 0.4 \pm 0.1$
N_i^{bkg}	$2.9 \pm 0.6 \pm 0.1$	$2.9 \pm 0.6 \pm 0.2$
$\varepsilon_i^{\text{sig}} (\times 10^{-5})$	$43.8 \pm 0.7 \pm 3.0$	$10.3 \pm 0.2 \pm 1.2$
N_i^{obs}	6	3
\mathcal{B}_i	$(1.5^{+1.7+0.4}_{-0.8-0.2}) \times 10^{-5}$	$(0.14^{+6.0+1.7}_{-1.9-0.9}) \times 10^{-5}$
Limits	$(> 0.4, < 3.7) \times 10^{-5}$	$< 8.1 \times 10^{-5}$
$\mathcal{B}(B \rightarrow K \nu \bar{\nu})$	$(1.4^{+1.4+0.3}_{-0.9-0.2}) \times 10^{-5}$	
Limits	$(> 0.2, < 3.2) \times 10^{-5}$	

90% CL of

$$\begin{aligned} \mathcal{B}(B^+ \rightarrow K^{*+} \nu \bar{\nu}) &< 6.4 \times 10^{-5}, \\ \mathcal{B}(B^0 \rightarrow K^{*0} \nu \bar{\nu}) &< 12 \times 10^{-5}, \text{ and} \\ \mathcal{B}(B \rightarrow K^* \nu \bar{\nu}) &< 7.6 \times 10^{-5}. \end{aligned} \quad (5)$$

The combined central value is $\mathcal{B}(B \rightarrow K^* \nu \bar{\nu}) = (3.8^{+2.9}_{-2.6}) \times 10^{-5}$.

Since certain new-physics models suggest that enhancements are possible at high s_B values, we also report model-independent partial branching fractions ($\Delta \mathcal{B}_i$) over the full s_B spectrum by removing the low- s_B requirement. The $\Delta \mathcal{B}_i$ values are calculated in intervals of $s_B = 0.1$, using Eq. (3) (with the N_i^{obs} , N_i^{peak} , N_i^{comb} , and $\varepsilon_i^{\text{sig}}$ values found within the given interval) multiplied

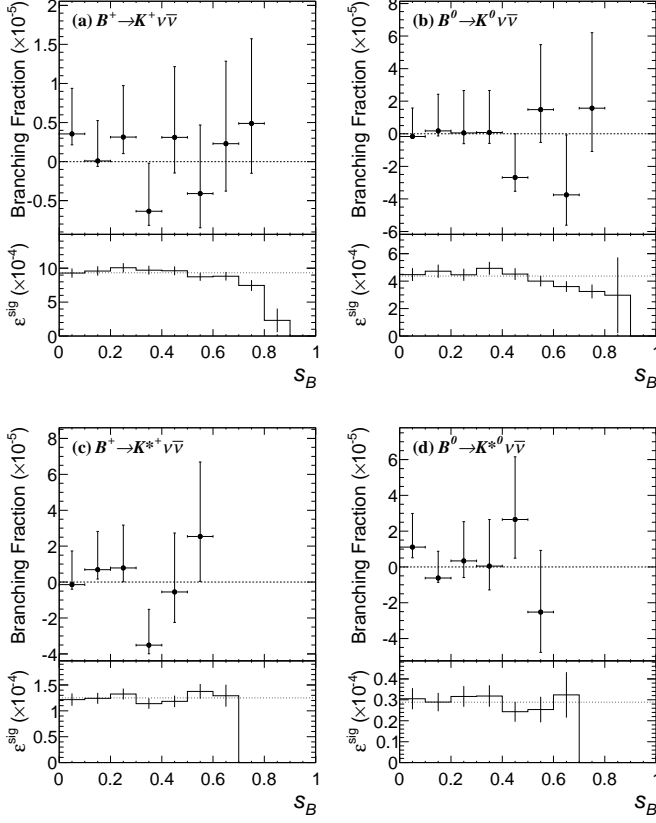


FIG. 5: The central values (points with 1σ error bars) of the partial branching fractions $\Delta\mathcal{B}_i$ versus s_B , for (a) $B^+ \rightarrow K^+ \nu \bar{\nu}$, (b) $B^0 \rightarrow K^0 \nu \bar{\nu}$, (c) $B^+ \rightarrow K^{*+} \nu \bar{\nu}$, and (d) $B^0 \rightarrow K^{*0} \nu \bar{\nu}$. The subplots show the distribution of the final signal efficiencies within each s_B interval (histogram with error bars), and the value of the total signal efficiency after applying all selection criteria without any requirement on s_B (dotted line). The partial branching fractions are provided only within the intervals that are unaffected by the kinematic limit at large s_B .

by the fraction of the signal efficiency distribution inside that interval. Figure 5 shows the partial branching fractions. The signal efficiency distributions are relatively independent of s_B , which are also illustrated in Fig. 5. To compute model-specific values from these results, one can sum the central values within the model's dominant interval(s) (with uncertainties added in quadrature) and divide the sum by the fraction of the model's distribution that is expected to lie within the same s_B intervals. These partial branching fractions provide branching fraction upper limits for several new-physics scenarios at the level of 10^{-5} .

The $B \rightarrow K^{(*)} \nu \bar{\nu}$ decays are also sensitive to the short-distance Wilson coefficients $|C_{L,R}^\nu|$ for the left- and right-handed weak currents, respectively. These couple two quarks to two neutrinos via an effective field theory point interaction [32]. Although $|C_R^\nu| = 0$ within the SM, right-

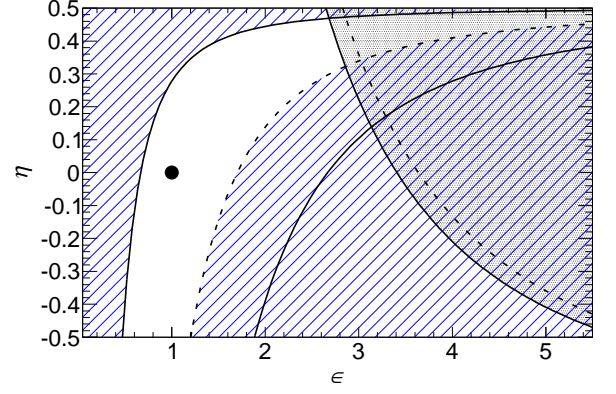


FIG. 6: The constraints at 90% CL on ϵ and η for sensitivity to new physics with right-handed currents. The $B \rightarrow K \nu \bar{\nu}$ (diagonal shading) and $B \rightarrow K^* \nu \bar{\nu}$ (grey shading) excluded areas are determined from the upper and lower limits of this $B \rightarrow K^{(*)} \nu \bar{\nu}$ analysis (solid curves), and from the most-stringent upper limits from previous semileptonic-tag analyses [17, 18] (dashed curves). The dot shows the expected SM value.

handed currents from new physics, such as non-SM Z^0 penguin couplings, could produce non-zero values. Using the parameterization from Ref. [1],

$$\epsilon \equiv \frac{\sqrt{|C_L^\nu|^2 + |C_R^\nu|^2}}{|C_{L,SM}^\nu|}, \quad \eta \equiv \frac{-\text{Re}(C_L^\nu C_R^{*\nu})}{|C_L^\nu|^2 + |C_R^\nu|^2}, \quad (6)$$

the $B \rightarrow K^* \nu \bar{\nu}$ upper limits from this search improve the constraints from previous searches on the Wilson-coefficient parameter space, as shown in Fig. 6. The $B \rightarrow K \nu \bar{\nu}$ lower limit provides the first upper bound on η and lower bound on ϵ . These constraints are consistent with the expected SM values of $\epsilon = 1$ and $\eta = 0$.

RESULTS FOR $c\bar{c} \rightarrow \nu \bar{\nu}$

In the search for $c\bar{c} \rightarrow \nu \bar{\nu}$, Fig. 7 shows the $m_{\nu \bar{\nu}}$ distribution of the observed data yields, expected background contributions, and SM signal distributions. Tables VI and VII summarize the background contribution values and signal efficiencies within the J/ψ and $\psi(2S)$ invariant mass regions. The Tables also report the combined branching fraction central values and the branching fraction upper limits at 90% CL for $J/\psi \rightarrow \nu \bar{\nu}$ and $\psi(2S) \rightarrow \nu \bar{\nu}$. The signal efficiencies account for the $B \rightarrow K^{(*)} J/\psi$ and $B \rightarrow K^{(*)} \psi(2S)$ branching fractions and their errors, which are taken from Ref. [29]. The data yield is consistent with zero observed $c\bar{c} \rightarrow \nu \bar{\nu}$ signal events in all channels.

The combined upper limits for the charmonium

TABLE VI: Expected $J/\psi \rightarrow \nu\bar{\nu}$ background yields N_i^{peak} and N_i^{bkg} , signal efficiencies $\varepsilon_i^{\text{sig}}$, number of observed data events N_i^{obs} , and the resulting branching fraction central value and upper limit at 90% CL, all within the $m_{\nu\bar{\nu}}$ invariant mass region corresponding to the J/ψ mass. Uncertainties are statistical and systematic, respectively. The N_i^{comb} yields are calculable as $N_i^{\text{bkg}} - N_i^{\text{peak}}$.

Channel	$J/\psi \rightarrow \nu\bar{\nu}$					
	K^+	K^0	$K^{*+} \rightarrow K^+\pi^0$	$K^{*+} \rightarrow K_S^0\pi^+$	$K^{*0} \rightarrow K^+\pi^-$	$K^{*0} \rightarrow K_S^0\pi^0$
N_i^{peak}	$0.4 \pm 0.2 \pm 0.0$	$0.7 \pm 0.3 \pm 0.1$	$0.8 \pm 0.3 \pm 0.1$	$0.4 \pm 0.2 \pm 0.0$	$2.6 \pm 0.5 \pm 0.3$	$0.6 \pm 0.2 \pm 0.1$
N_i^{bkg}	$0.5 \pm 0.2 \pm 0.0$	$0.7 \pm 0.3 \pm 0.1$	$0.8 \pm 0.3 \pm 0.1$	$0.8 \pm 0.3 \pm 0.0$	$2.8 \pm 0.5 \pm 0.3$	$0.6 \pm 0.2 \pm 0.1$
$\varepsilon_i^{\text{sig}} (\times 10^{-8})$	$95.3 \pm 4.4 \pm 5.5$	$19.3 \pm 1.0 \pm 2.1$	$20.9 \pm 1.5 \pm 1.7$	$12.4 \pm 0.8 \pm 1.0$	$36.2 \pm 1.9 \pm 4.0$	$1.8 \pm 0.2 \pm 0.2$
N_i^{obs}	1	0	1	0	0	1
$\mathcal{B}(J/\psi \rightarrow \nu\bar{\nu})$	$(0.2^{+2.7+0.5}_{-0.9-0.4}) \times 10^{-3}$					
Limit	$< 3.9 \times 10^{-3}$					

TABLE VII: Expected $\psi(2S) \rightarrow \nu\bar{\nu}$ background yields N_i^{peak} and N_i^{bkg} , signal efficiencies $\varepsilon_i^{\text{sig}}$, number of observed data events N_i^{obs} , and the resulting branching fraction central value and upper limit at 90% CL, all within the $m_{\nu\bar{\nu}}$ invariant mass region corresponding to the $\psi(2S)$ mass. Uncertainties are statistical and systematic, respectively. The N_i^{comb} yields are calculable as $N_i^{\text{bkg}} - N_i^{\text{peak}}$.

Channel	$\psi(2S) \rightarrow \nu\bar{\nu}$					
	K^+	K^0	$K^{*+} \rightarrow K^+\pi^0$	$K^{*+} \rightarrow K_S^0\pi^+$	$K^{*0} \rightarrow K^+\pi^-$	$K^{*0} \rightarrow K_S^0\pi^0$
N_i^{peak}	$1.4 \pm 0.4 \pm 0.1$	$0.6 \pm 0.3 \pm 0.1$	$1.4 \pm 0.4 \pm 0.1$	$1.0 \pm 0.3 \pm 0.1$	$3.5 \pm 0.7 \pm 0.3$	$0.6 \pm 0.2 \pm 0.1$
N_i^{bkg}	$1.6 \pm 0.4 \pm 0.1$	$0.7 \pm 0.3 \pm 0.1$	$1.4 \pm 0.4 \pm 0.1$	$1.5 \pm 0.4 \pm 0.1$	$3.9 \pm 0.7 \pm 0.3$	$0.6 \pm 0.2 \pm 0.1$
$\varepsilon_i^{\text{sig}} (\times 10^{-8})$	$57.2 \pm 3.5 \pm 3.3$	$13.1 \pm 1.2 \pm 1.4$	$8.1 \pm 1.7 \pm 0.7$	$4.9 \pm 1.1 \pm 0.4$	$14.2 \pm 1.2 \pm 1.6$	$0.6 \pm 0.1 \pm 0.1$
N_i^{obs}	3	1	1	3	5	1
$\mathcal{B}(\psi(2S) \rightarrow \nu\bar{\nu})$	$(5.6^{+7.4+1.6}_{-4.6-1.4}) \times 10^{-3}$					
Limit	$< 15.5 \times 10^{-3}$					

branching fraction values are determined to be

$$\frac{\mathcal{B}(J/\psi \rightarrow \nu\bar{\nu})}{\mathcal{B}(J/\psi \rightarrow e^+e^-)} < 6.6 \times 10^{-2} \text{ and } \frac{\mathcal{B}(\psi(2S) \rightarrow \nu\bar{\nu})}{\mathcal{B}(\psi(2S) \rightarrow e^+e^-)} < 2.0, \quad (7)$$

where $\mathcal{B}(J/\psi \rightarrow e^+e^-)$ and $\mathcal{B}(\psi(2S) \rightarrow e^+e^-)$ are taken from Ref. [29]. With the addition of a new-physics U boson, these ratios would be proportional to $|f_{cV}c_{\chi,\varphi}|$, where $c_{\chi,\varphi}$ and f_{cV} are the U couplings to the LDM particles χ or φ and to the c -quark respectively [13]. The J/ψ decay ratio yields upper limits at 90% CL of $|f_{cV}c_{\chi,\varphi}| < (3.0, 2.1, 1.5) \times 10^{-2}$ for spin-0, Majorana, and Dirac LDM particles respectively. These limits are comparable with those obtained by BES for $J/\psi \rightarrow \nu\bar{\nu}$, in $\psi(2S) \rightarrow \pi^+\pi^- J/\psi$ [19].

SUMMARY

In conclusion, we have searched for the decays $B \rightarrow K\nu\bar{\nu}$ and $B \rightarrow K^*\nu\bar{\nu}$, as well as $J/\psi \rightarrow \nu\bar{\nu}$ and $\psi(2S) \rightarrow \nu\bar{\nu}$ via $B \rightarrow K^{(*)}J/\psi$ and $B \rightarrow K^{(*)}\psi(2S)$, recoiling from a hadronically reconstructed B meson within

a data sample of $471 \times 10^6 B\bar{B}$ pairs. We observe no significant signal in any of the channels and obtain upper limits at the 90% CL of $\mathcal{B}(B \rightarrow K\nu\bar{\nu}) < 3.2 \times 10^{-5}$, $\mathcal{B}(B \rightarrow K^*\nu\bar{\nu}) < 7.9 \times 10^{-5}$, $\mathcal{B}(J/\psi \rightarrow \nu\bar{\nu}) < 3.9 \times 10^{-3}$, and $\mathcal{B}(\psi(2S) \rightarrow \nu\bar{\nu}) < 15.5 \times 10^{-3}$. The branching fraction central values and upper limits are consistent with SM predictions. We report $B \rightarrow K^{(*)}\nu\bar{\nu}$ branching fraction limits in Tables IV and V, and $c\bar{c} \rightarrow \nu\bar{\nu}$ branching fraction limits in Tables VI and VII. These results include the first lower limit in the $B^+ \rightarrow K^+\nu\bar{\nu}$ decay channel, the most stringent published upper limits using the hadronic-tag reconstruction technique in the $B^0 \rightarrow K^0\nu\bar{\nu}$, $B^+ \rightarrow K^{*+}\nu\bar{\nu}$, and $B^0 \rightarrow K^{*0}\nu\bar{\nu}$ channels, and the first upper limit for $\psi(2S) \rightarrow \nu\bar{\nu}$. We also present partial branching fraction values for $B \rightarrow K^{(*)}\nu\bar{\nu}$ over the full s_B spectrum in Fig. 5 in order to enable additional tests of new-physics models.

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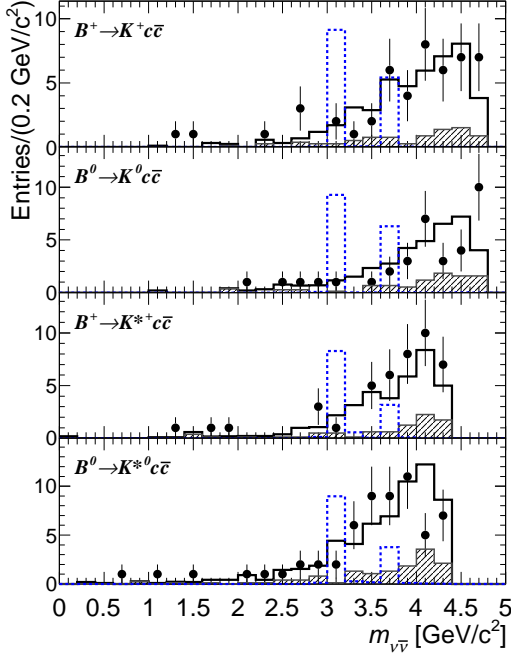


FIG. 7: The $m_{\nu\bar{\nu}} \equiv \sqrt{s_B m_B^2}$ distribution for (from top to bottom) $B^+ \rightarrow K^+ c\bar{c}$, $B^0 \rightarrow K^0 c\bar{c}$, $B^+ \rightarrow K^{*+} c\bar{c}$, and $B^0 \rightarrow K^{*0} c\bar{c}$ events after applying the full signal selection. The expected combinatorial (shaded) plus m_{ES} -peaking (solid) background contributions are overlaid on the data (points). The signal MC distributions (dashed) are normalized to $\mathcal{B}(c\bar{c} \rightarrow \nu\bar{\nu})$ values of 2% for the K^+ channel, 10% for the K^0 channel, and 5% for the K^* channels.

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